

- $\mathbf{n}$  : matrix  $\mathbf{N}$  of integers  $\geq 1$ .
- $\mathbf{p}$  : matrix  $\mathbf{P}$  of integers of the same size as  $\mathbf{N}$ . Each element  $p_i$  of  $\mathbf{P}$  must verify  $0 \leq p_i \leq n_i$ .
- $\mathbf{c}$  : matrix  $\mathbf{C}$  of integers.

### Description

Compute in matrix  $\mathbf{C}$  the combinations  $C_n^p$  for each elements of matrices  $\mathbf{N}$  and  $\mathbf{P}$ .

### Examples

```
c=combination(10*ones(1,10+1)',(0:10)';
mprintf("C(10,%2d) = %d\n",[(0:10)',c])
```

## 6.5 depth - multivariate depth

### Calling Sequence

```
[d,id]=depth(x,dep)
[d,id]=depth(x,dep,y)
```

### Parameters

- $\mathbf{x}$  : real matrix  $\mathbf{X}$  of size  $(n_X, p)$ .
- $\mathbf{y}$  : real matrix  $\mathbf{Y}$  of size  $(n_Y, p)$ . Default is  $\mathbf{x}$ .
- $\mathbf{dep}$  : multivariate definition of depth in  $\mathbb{R}^p$ . Must be "halfspace", "majority" or "simplicial".
- $\mathbf{d}$  : column vector  $\mathbf{d}$  of depths.
- $\mathbf{id}$  : vector of indices corresponding to the depths sorted in descending order.

### Description

Compute in vector  $\mathbf{d}$  the depths for each row vector of matrix  $\mathbf{Y}$  based on row vectors in matrix  $\mathbf{X}$ . The indices corresponding to the depths sorted in descending order are in  $\mathbf{id}$ , i.e.  $\mathbf{x}(\mathbf{id}(1), :)$  is a potential multivariate median.  $[\mathbf{d}, \mathbf{id}] = \text{depth}(\mathbf{x}, \mathbf{dep})$  is equivalent to  $[\mathbf{d}, \mathbf{id}] = \text{depth}(\mathbf{x}, \mathbf{dep}, \mathbf{x})$ .

### Examples

```
x=rdmultinormal(100,[0,0],[2,1.9;1.9,5]);
[d1,id1]=depth(x,"halfspace");
[d2,id2]=depth(x,"majority");
[d3,id3]=depth(x,"simplicial");
//
xset("window",0)
xbasc();plot2d(x(:,1),x(:,2),-6)
xset("color",4)
plot2d(x(id1(1:20),1),x(id1(1:20),2),-6)
```

```

xset("color",5)
plot2d(x(id1(81:100),1),x(id1(81:100),2),-6)
xset("color",0);xtitle("HALFSPACE MULTIVARIATE DEPTH");xselect()
//
xset("window",1)
xbasc();plot2d(x(:,1),x(:,2),-6)
xset("color",4)
plot2d(x(id2(1:20),1),x(id2(1:20),2),-6)
xset("color",5)
plot2d(x(id2(81:100),1),x(id2(81:100),2),-6)
xset("color",0);xtitle("MAJORITY MULTIVARIATE DEPTH");xselect()
//
xset("window",2)
xbasc();plot2d(x(:,1),x(:,2),-6)
xset("color",4)
plot2d(x(id3(1:20),1),x(id3(1:20),2),-6)
xset("color",5)
plot2d(x(id3(81:100),1),x(id3(81:100),2),-6)
xset("color",0);xtitle("SIMPLICIAL MULTIVARIATE DEPTH");xselect()

```

## 6.6 hausdorff - Hausdorff distance between polylines

### Calling Sequence

```

h=hausdorff(x,y)
h=hausdorff(x,y,q)

```

### Parameters

- **x** : real matrix **X** of size  $(n_X, p)$ .
- **y** : real matrix **Y** of size  $(n_Y, p)$ .
- **q** : quantile  $q$  used for the Hausdorff distance. Default is 0.5, i.e. the sample median.
- **h** : Hausdorff distance between polylines **X** and **Y**.

### Description

Compute the Hausdorff distance between polylines **X** and **Y** using the Euclidean distance.

### Examples

```

x=linspace(-%pi,%pi)';
y1=sin(x)+rdnormal(100,sigma=0.1);
y2=sin(x)+rdnormal(100,sigma=0.1);
y3=sin(2*x)+rdnormal(100,sigma=0.1);
hausdorff([x,y1],[x,y2])
hausdorff([x,y1],[x,y3])

```